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A nonparametric model for sensors used in a dynamic context

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Steady state or static conditions

Steady state

- \blacktriangleright Calibration procedure and uncertainty budget: well defined
- \blacktriangleright Example: calibration of 2 temperature sensors (Pt100 type)

Dispersion of sensors in static conditions

Steady state

- \blacktriangleright 2 sets of Pt100 probes:
	- $\mathcal{L}_{\mathcal{A}}$ \varnothing = 6 mm and \varnothing = 3 mm
	- $\mathcal{L}_{\mathcal{A}}$ Calibrated between +10°C and 90°C

Experimental setup

Sensor response to a step excitation

Unsteady state

- \blacktriangleright Real measurement are often unsteady
- \blacktriangleright Example: **step excitation** in temperature, **1 probe**

Sensor response to a step excitation

Unsteady state

- \blacksquare Real measurement are often unsteady
- \blacktriangleright Example: **step excitation** in temperature, **1 probe**

Sensor response to a step excitation

Unsteady state

- \mathbf{r} Real measurement are often unsteady
- \blacktriangleright Example: step excitation in temperature, **several probes**

Model based approach for uncertainty propagation LNE

Particularly strong issues in industrial cases :

- It may be hard to find an accurate model of a sensor with a small number of parameters θ
- the excitation is often unknown or not well characterized

Measured signals for a set of 20 sensors

Simulation of observed data obtained by :

- arbitrary choice of the excitation signal *u(t)*
- considering sensors with different time constants

Modeling the sensor response

- •The model of the response is unknown
- • The observed signals suggest that the output trajectories are variations around a mean behaviour
- \bullet The number of tested sensors is small
- • In the case of fluctuations varying slowly in time, it's no longer valid to consider that the errors at two different times are independent

Statistical model and inference

The response *Yobs* is modeled as a sum of :

- a Gaussian process *M* invariant through the sensors representing the nominal behaviour
- Gaussian processes μ specific to each sensor \bm{j} , representing the departure from the nominal behaviour due to specific values of the conception parameters
- a random noise ε i.i.d. at each time t_k , with the sensor j and the repetition i

$$
Y_{i,j,k}^{obs} = M(t_k) + \mu_j(t_k) + \varepsilon_{i,j,k}
$$

$$
\varepsilon_{i,j,k} \sim N(0,\sigma^2)
$$

The model parameters are then estimated by likelihood maximisation

Considering the statistical model estimated, Monte Carlo simulations are performed to compute trajectories of the sensors

With 5 trajectories picked from the set of simulated trajectories

With 20 trajectories picked from the set of simulated trajectories

With 100 trajectories picked from the set of simulated trajectories

With the all set of simulated trajectories (10000 trajectories)

Coverage region

Defining a coverage region at a given level α R_{α} is a coverage region, defined such that : $\mathbb{P}(\forall t \in \mathbb{T}, Y(t) \in R_{\alpha}) = \alpha$

This region must contain α % of the trajectories

Proposal definition of the confidence region LNE

Non unique way to define a coverage region Proposed process :

1.To obtain confidence intervals \mathbf{CI}_β at each instant t

2.To define coverage region of level α based on these intervals

Mathematical definition of the coverage region \boldsymbol{R}_{α}

is a coverage region if, $t \in T, P(Y(t) \in R_{\alpha}) = \text{constant}$

 $R_{CI_{\beta}} = U_{t\in T}\left\{CI_{\beta}(t)\right\}$ $=$ U $_{t \in$

defines a coverage region of level $\;\;\alpha = g(\beta)$ \leq β

- Empirical estimation of the function $g(\beta)$
- Inversion of the function leads to find, for a desired level α , the value of β to be used

The red star indicates the value of β for α = 95%

Construction of the coverage region R_α

Coverage region of level α = 95%

Adequacy between observed trajectories and R

LNE

Quality control of the sensors

Among all simulations of sensors responses according to their own time constant, let's focus on two particular sensors A and B

Identification of sensors *A* **and** *B*

The cut-off frequency is the inverse of the time constant of the sensor

Sensor *A* has an expected frequency in the intermediate range such as all the sensors in green whose trajectories belong to the coverage region

On the contrary, sensor B has a low frequency, indicating an inaccurate behaviour, like almost all the sensors outside the coverage region

Conclusion

- • Proposal to characterize measurement uncertainty for dynamic measurement based on the concept of coverage region
- • The estimation of the coverage region requires a statistical model of the sensor output
- • The statistical model developed allows to catch both the mean behaviour and the magnitude of the departures from the mean behaviour
- \bullet A prior model of the sensor is not required
- • Gaussian process is a suitable statistical tool to take into account the time dependence

Non utile ? Estimated mean behavior. Additional supplied information: confidence area for the mean behavior

