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### A nonparametric model for sensors used in a dynamic context

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## **Steady state or static conditions**



#### Steady state

- Calibration procedure and uncertainty budget: well defined
- Example: calibration of 2 temperature sensors (Pt100 type)



### **Dispersion of sensors in static conditions**



### Steady state

- 2 sets of Pt100 probes:
  - Ø= 6 mm and Ø= 3 mm
  - Calibrated between +10°C and 90°C



## **Experimental setup**







## Sensor response to a step excitation



#### Unsteady state

- Real measurement are often unsteady
- Example: **step excitation** in temperature, **1 probe**



## Sensor response to a step excitation



#### Unsteady state

- Real measurement are often unsteady
- Example: **step excitation** in temperature, **1 probe**



## Sensor response to a step excitation

#### Unsteady state

- Real measurement are often unsteady
- Example: step excitation in temperature, **several probes**



## Model based approach for uncertainty propagation LNE



Particularly strong issues in industrial cases :

- $\bullet$  It may be hard to find an accurate model of a sensor with a small number of parameters  $\theta$
- the excitation is often unknown or not well characterized



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## Measured signals for a set of 20 sensors



Simulation of observed data obtained by :

- arbitrary choice of the excitation signal *u*(*t*)
- considering sensors with different time constants





## **Modeling the sensor response**



- The model of the response is unknown
- The observed signals suggest that the output trajectories are variations around a mean behaviour
- The number of tested sensors is small
- In the case of fluctuations varying slowly in time, it's no longer valid to consider that the errors at two different times are independent



## **Statistical model and inference**



The response **Y**<sup>obs</sup> is modeled as a sum of :

- a Gaussian process *M* invariant through the sensors representing the nominal behaviour
- Gaussian processes  $\mu$  specific to each sensor **j**, representing the departure from the nominal behaviour due to specific values of the conception parameters
- a random noise  $\varepsilon$  i.i.d. at each time  $t_k$ , with the sensor j and the repetition i

$$Y_{i,j,k}^{obs} = M(t_k) + \mu_j(t_k) + \mathcal{E}_{i,j,k}$$

$$\mathcal{E}_{i,j,k} \sim N(0,\sigma^2)$$

#### The model parameters are then estimated by likelihood maximisation



Considering the statistical model estimated, Monte Carlo simulations are performed to compute trajectories of the sensors





#### With 5 trajectories picked from the set of simulated trajectories







#### With 20 trajectories picked from the set of simulated trajectories







#### With 100 trajectories picked from the set of simulated trajectories







#### With the all set of simulated trajectories (10000 trajectories)



### **Coverage region**



Defining a coverage region at a given level  $\alpha$  $R_{\alpha}$  is a coverage region, defined such that :  $\mathbb{P}(\forall t \in \mathbb{T}, Y(t) \in R_{\alpha}) = \alpha$ 



### Proposal definition of the confidence region & LN

Non unique way to define a coverage region <u>Proposed process :</u>

1. To obtain confidence intervals  $\operatorname{CI}_{\beta}$  at each instant t

2.To define coverage region of level  $\boldsymbol{\alpha}$  based on these intervals



## Mathematical definition of the coverage region $R_{\alpha}$ LNE

 $\mathbf{R}_{\alpha}$  is a coverage region if,  $t \in T, P(Y(t) \in R_{\alpha}) = \text{constant}$ 

 $R_{CI_{\beta}} = U_{t \in T} \left\{ CI_{\beta}(t) \right\}$ 

defines a coverage region of level  $\alpha = g(\beta) \le \beta$ 

- Empirical estimation of the function  $g(\beta)$
- Inversion of the function leads to find, for a desired level  $\alpha$ , the value of  $\beta$  to be used

The red star indicates the value of  $\beta$  for  $\alpha = 95\%$ 





## Construction of the coverage region $R_{\alpha}$







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## Coverage region of level $\alpha = 95\%$







## Adequacy between observed trajectories and $R_{\alpha}$ & LNB





### **Quality control of the sensors**



Among all simulations of sensors responses according to their own time constant, let's focus on two particular sensors A and B





## Identification of sensors A and B



The cut-off frequency is the inverse of the time constant of the sensor

Sensor *A* has an expected frequency in the intermediate range such as all the sensors in green whose trajectories belong to the coverage region



On the contrary, sensor B has a low frequency, indicating an inaccurate behaviour, like almost all the sensors outside the coverage region

## Conclusion



- Proposal to characterize measurement uncertainty for dynamic measurement based on the concept of coverage region
- The estimation of the coverage region requires a statistical model of the sensor output
- The statistical model developed allows to catch both the mean behaviour and the magnitude of the departures from the mean behaviour
- A prior model of the sensor is not required
- Gaussian process is a suitable statistical tool to take into account the time dependence







### Non utile ? Estimated mean behavior. Additional supplied information: confidence area for the mean behavior



