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An efficient interpolation for calculation of the response of composite layered material and its implementation in MUSIC imaging



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Research context –

Main institutions involved

- Département de Recherche en Électromagnétisme, Laboratoire des Signaux et Systèmes UMR8506
- Department of Electrical and Computer Engineering, National University of Singapore

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Main financial support

Damaged structure

reflection/transmission

or at interfaces

- Bilateral Merlion Project (2011–2012), projet N^o 8.14.10 "Fast 3-D electromagnetic imaging of anisotropic media and non-destructive evaluation"
- DIGITEO : PhD Scholarship jointly involving L2S and CEA-LIST (Département Imagerie et Simulation pour le Contrôle)
- Univ Paris-Sud : invited assistant-professor
- Internal ressources (DRÉ & NUS)

• E.M. parameters differ from background stratified panel within layers

• 3-D volumetric defects (voids, fluid-filled cavities, localized damaged

zones, etc.), or delaminations (thin, air-type slabs)

formulations, or change of dyads via supplementary

Method of Moments upon vector contrast-source integral



To build

• Accurate computational models of complex anisotropic multi-layer composite panels • Robust, fast, end-user's friendly imaging procedures





NdT-E from eddy-currents to microwaves in aeronautics and automotive industries





Electromagnetic modeling and preliminary numerical results

Undamaged structure



- Each layer: homogeneous anisotropic (different e.m. properties from layer to next)
- Uniaxial dielectric (glass-based) or conductive (graphite-based) effective media *large-scale hypothesis*
- *Diagonal* tensor in eigenframes along and orthogonal to fibers' axes • Dyadic Green function in need as well as response to known distributed electric source anywhere in the structure

 $\bar{\bar{\varepsilon}}(\bar{r}) = \text{diag}\left[\varepsilon_{n;11}; \varepsilon_{n;22}(\bar{r}); \varepsilon_{n;22}(\bar{r})\right]$ in local coordinate system

Constructing the spectral and spatial response of the laminate (forward modeling)



- To efficiently calculate the spectral response of the laminate • Capable of stably dealing with distributed source along z More efficient compared to the traditional Green's function method
- To numerically solve the state equation
- d - $\frac{d}{dz}\bar{\psi}(z) = \bar{A}_{n} \cdot \bar{\psi}(z) + \bar{f}(z) \text{ with } \bar{\psi}(z) \text{ containing the tangential}$ components of the fields and $\overline{f}(z)$ being the source term



Figure : Reproduction of the results found in [2]

- Fast algorithm to calculate the spatial response of the laminate [7] • To efficiently calculate the spatial response on the rectilinear mesh
- No inverse Fourier transform involved
- Much faster than the inverse Fourier transform
- Incorporating the fast numerical interpolation and integration based on Padua points
- Especially useful when constructing the impedance matrix of the MoM

MUltiple SIgnal Classification (MUSIC) imaging with anisotropic layered media

Interpolation and integration using the Padua points

Dealing with fast oscillating integrals

(2)

(3)

1000

600

• Alternative representation as self intersections and boundary contacts of the generating curve $\gamma(t) = (-\cos((n+1)t), -\cos(nt), t \in [0,\pi])$



Figure : The Padua points with their generating curve for n = 12 (left, 91 points) and n = 13 (right, 105 points), also as union of two Chebyshev-Lobatto sub-grids (red and blue bullets). Image taken from [3].

• Goal is to compute the I-FT of fast oscillating spectrum in the $k_X - k_V$ plane

$$G(x, y) = \frac{1}{4\pi^2} \iint_{-\infty}^{\infty} \tilde{G}_0(k_x, k_y) e^{\left(ik_x x + ik_y y\right)} dk_x dk_y$$
(1)

• Interpolation of the non-oscillating part at the Padua points with Chebyshev's polynomial interpolant

$$\mathcal{L}_{n}\tilde{G}_{0}(k_{x},k_{y}) = \sum_{k=0}^{n} \sum_{j=0}^{k} c_{j,k-j}\hat{T}_{j}(k_{x})\hat{T}_{k-j}(k_{y}) - \frac{1}{2}c_{n,0}\hat{T}_{n}(k_{x})T_{0}(k_{y})$$

with weights $c_{j, k-j}$ computed using [4] • Fourier transform of Chebyshev polynomials given by

 $\hat{T}_n(k_x) \exp(-ik_x x) \,\mathrm{d}k_x$

are managed using [6] among other good options.

MUSIC images of anisotropic layered media affected by two defects



• Standard MUSIC imaging method [1]

$$\phi(\bar{r}) = \frac{1}{\sum_{\sigma_j < \sigma_L} \sum_{\nu=1}^3 \left| \bar{u}_j^* \cdot \bar{G}_{\nu}(\bar{r}) \right|^2}$$

Enhanced MUSIC imaging method [5]







• A cross type antenna array with 5 antennas on each arm. Each antenna as transceivers with x and y polarizations. • Two small inclusions with dimension of $0.1\lambda_0 \times 0.1\lambda_0 \times 0.1\lambda_0$.

 $\bar{\bar{\epsilon}}_{b1} = \text{diag} [4.5 + i0.2, 6 + i0.05, 6 + i0.05]; \theta_{b1} = 45^{\circ}$ $\bar{\bar{\epsilon}}_{b2} = \text{diag} \left[2 + i0.3, 3 + i0.1, 3 + i0.1 \right]$ $heta_{b2} = 60^{\circ}$ $\overline{\overline{\epsilon}}_{S_1} = \overline{\overline{l}} \epsilon_0 \quad \theta_{S_1} = 0^\circ \quad \theta_{S_2} = 120^\circ$ $\overline{\overline{\epsilon}}_{S_2} = \text{diag} \left[4.5 + \text{i}0.2, 6 + \text{i}0.05, 6 + \text{i}0.05 \right] \quad l_1 = 0.5\lambda_0$ $(x_{s_2}, y_{s_2}, z_{s_2}) = (-0.2\lambda_0, -0.1\lambda_0, -0.55\lambda_0) I_2 = 0.2\lambda_0$ $(x_{s_1}, y_{s_1}, z_{s_1}) = (0.15\lambda_0, 0.2\lambda_0, -0.35\lambda_0)$ $I_3 = 0.2\lambda_0$





Conclusions & perspectives

•	Numerical integration method based on Padua points is proposed to avoid directly interpolating on the fast oscillating function. The approach is validated by comparison with configurations found in the literature	 Green's function constructed by the proposed method is applied in MUSIC imaging. Preliminary numerical results show the efficiency of the proposed method in a fully complex anisotropic configuration
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